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## Introduction

### Background

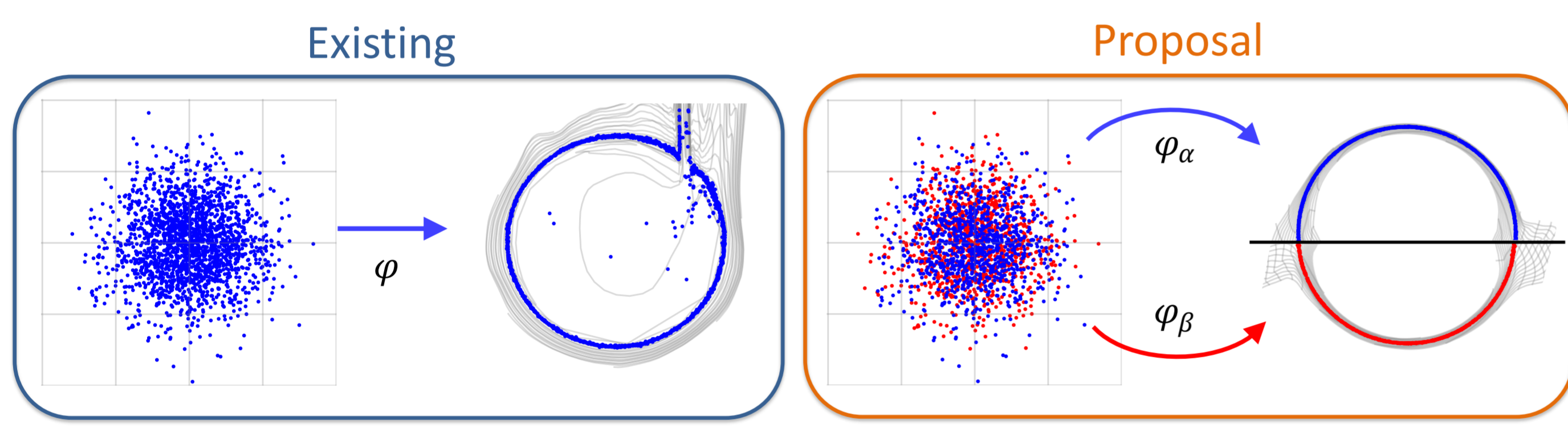
- A point cloud is becoming popular because it can capture high-resolution and is easier to manipulate.
- Point cloud generative model is useful for 3D computer vision tasks, such as shape completion, shape synthesis, and super-resolution.
- Most studies trained flow-based generative models to maximize the likelihood instead of a heuristic quality measurement of a generated point cloud.

### Difficulties

- A flow-based generative model fails in expressing a point cloud that has a manifold-like structure because
  - a bijective map does not exist between a Euclidean space and a manifold with holes.
  - a point cloud is often composed of multiple subparts, some of which are disconnected.

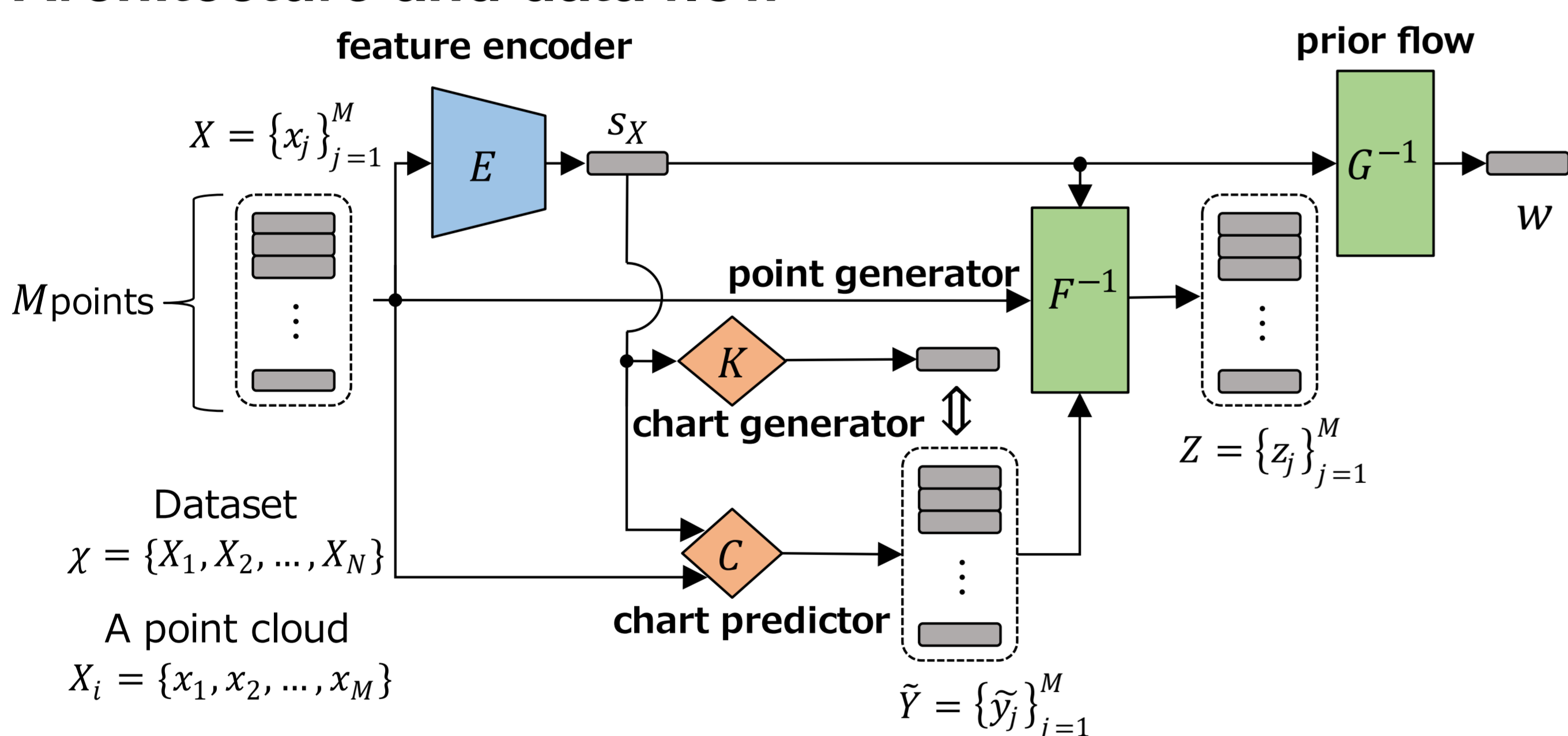
### Proposal

- We employed flow-based generative model using multiple latent labels, each of which is
  - assigned to a continuous subset of a given point cloud in unsupervised manner.
  - corresponding to a map, similarly to a chart of a manifold.
- A set of charts forms an atlas that covers the entire point cloud.



## Proposed Method

### Architecture and data flow



- ◊ The chart predictor infers the label  $y$  that corresponds to the chart that the point  $x$  belongs to.
- ◻ The point generator learns a set of maps, given the label as a condition.
- ◊ The chart generator learns the posterior  $p_K(y|s_X)$  of the label  $y$  for generation task.

### Objective

- The evidence lower bound (ELBO)

$$\begin{aligned} \log p(X) &\geq \mathbb{E}_{q_E(s_X|X)} \mathbb{E}_{q_C(y|X, s_X)} \left[ \log \frac{p_F(X|Y, s_X) p(Y) p_G(s_X)}{q_C(Y|X, s_X) q_E(s_X|X)} \right] \\ &= \mathbb{E}_{q_E(s_X|X)} \left[ \sum_j \left\{ \mathbb{E}_{q_C(y_j|x_j, s_X)} \left[ \log p_F(x_j|y_j, s_X) \right] \right. \right. \\ &\quad \left. \left. + H[q_C(y_j|x_j, s_X)] - H[q_C(y_j|x_j, s_X)|p(y_j)] \right\} \right] - D_{KL}(q_E(s_X|X) \| p_G(s_X)) \\ &=: \mathcal{L}_{ELBO}(F, C, E, G; X). \end{aligned}$$

- The regularization term to assign a map to a continuous subset

$$\mathcal{L}_{MI}(C; X, \mu, \lambda) = \sum_j \left\{ \mu H \left[ \frac{1}{|X|} \sum_{\tilde{x} \in X} q_C(y_j|\tilde{x}) \right] - \lambda H[q_C(y_j|x_j)] \right\}. \quad \mu, \lambda: \text{coefficient}$$

- The final objective function to be maximized

$$\mathcal{L}(F, C, E, G, K; \mathcal{X}, \mu, \lambda) = \sum_{X \in \mathcal{X}} \left[ \tilde{\mathcal{L}}_{ELBO} + \mathcal{L}_{MI} \right].$$

## Experiments

### Generation and Reconstruction

- Dataset: ShapeNet. [Chang+, arXiv2015]
  - Three categories: airplane, chair, and car. [Yang+, ICCV2019]

### Unsupervised Segmentation

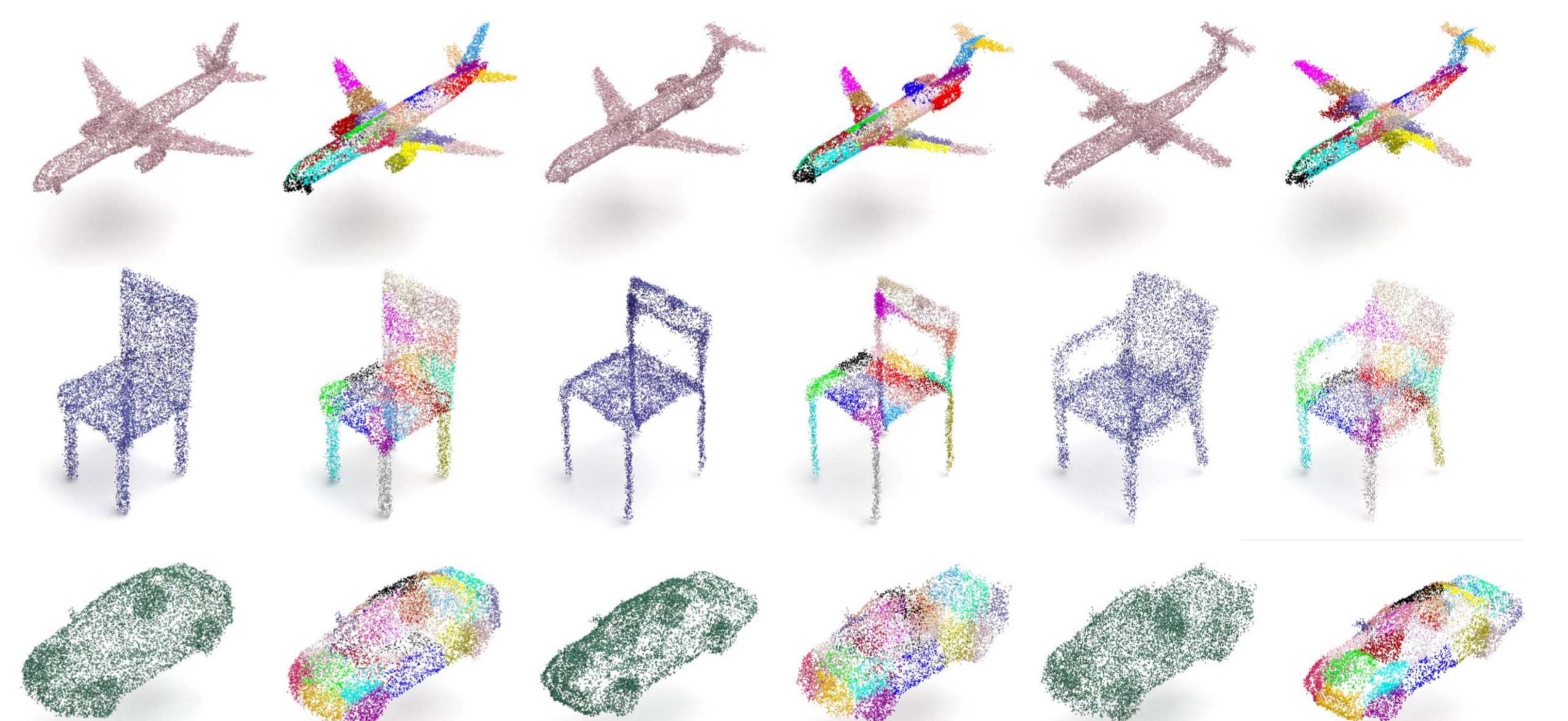
- Dataset: PartDataset. [Yi+, SIGGRAPH Asia2016]
  - Three categories: airplane, chair, and car.
  - divided into four parts.

## Results

### Generation (1-NNA, closer to 50% is better)

- ChartPointFlow outperformed other point cloud generators.

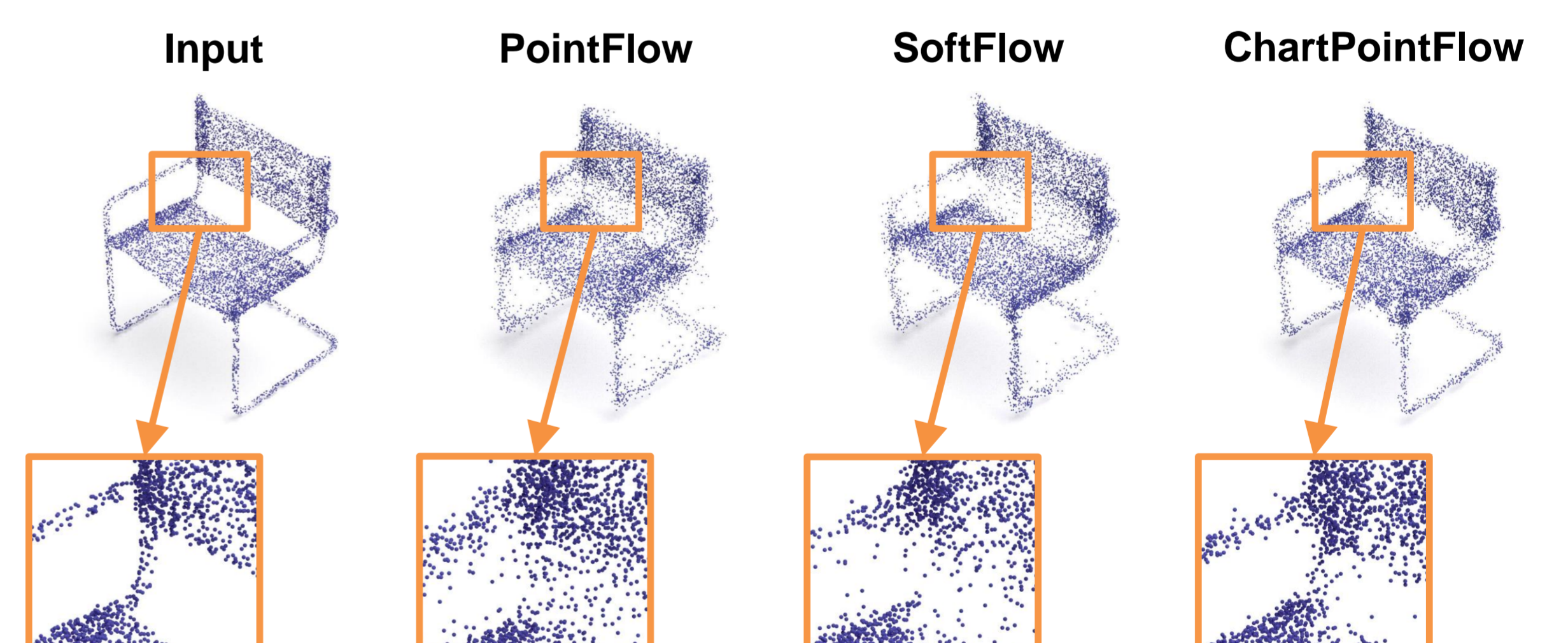
Model	Airplane	Chair	Car
I-GAN (EMD) [Achlioptas+, ICML2018]	85.68	65.56	68.32
PC-GAN [Li+, arXiv2018]	92.32	78.37	90.87
ShapeGF [Cai+, ECCV2020]	81.44	59.60	60.31
PointFlow [Yang+, ICCV2019]	75.06	59.89	62.36
SoftFlow [Kim+, NeurIPS2020]	69.44	63.51	64.71
ChartPointFlow (proposed)	<b>65.08</b>	<b>58.31</b>	<b>58.68</b>



Generation examples by ChartPointFlow (each color represents a chart).

### Reconstruction

- State-of-the-art (see the manuscript for numerical performances).
- The large improvement in the chair category, especially compared to models using flows, namely PointFlow and SoftFlow.

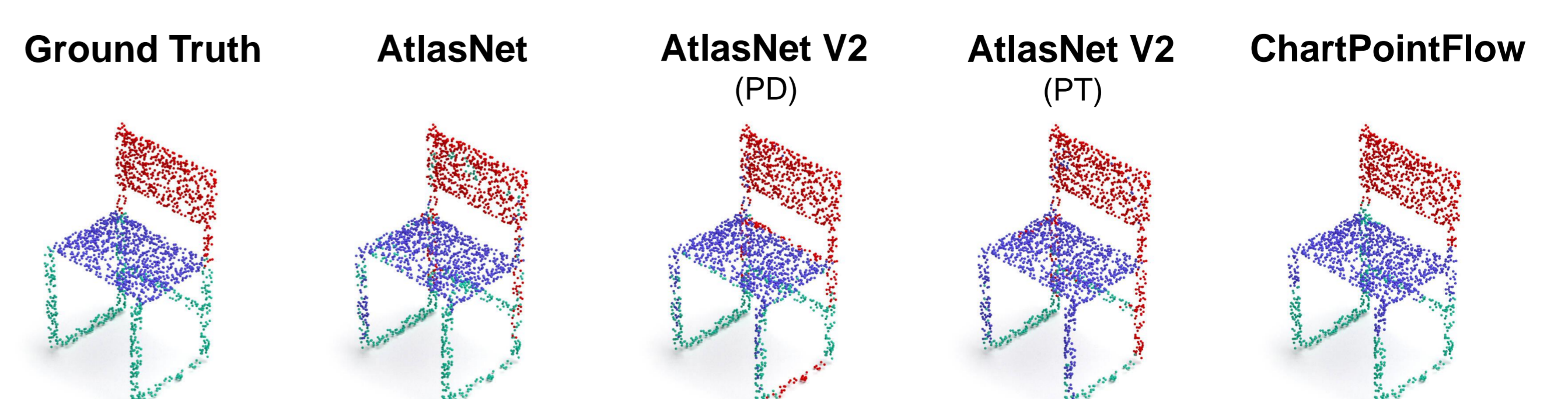


Reconstruction examples by each model.

### Unsupervised Segmentation (NMI / purity, larger is better)

- ChartPointFlow outperformed AtlasNets for both criteria in all categories, except for the purity of the airplane.

Model	Airplane	Chair	Car
AtlasNet [Groueix+, CVPR2018]	0.22 / 0.76	0.23 / 0.74	0.11 / 0.71
AtlasNet V2 (PD) [Deprelle, NeurIPS2019]	0.25 / 0.79	0.24 / 0.75	0.13 / 0.72
AtlasNet V2 (PT) [Deprelle, NeurIPS2019]	0.27 / <b>0.80</b>	0.24 / 0.74	0.17 / 0.73
ChartPointFlow (proposed)	<b>0.30 / 0.80</b>	<b>0.35 / 0.86</b>	<b>0.19 / 0.79</b>



Results of unsupervised segmentation.